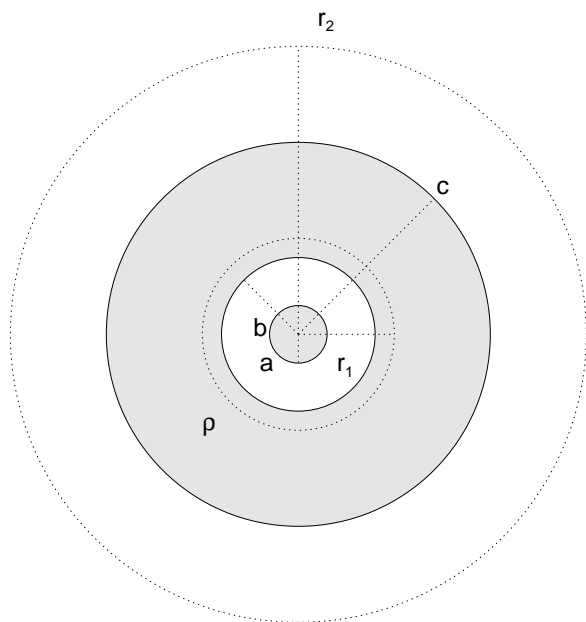


$ E(r)  = \frac{q}{4\pi\epsilon_0 r^2}$	$ E(r)  = \frac{\lambda}{2\pi\epsilon_0 r}$	$ E  = \frac{\sigma}{2\epsilon_0}$
$V(r) = \frac{q}{4\pi\epsilon_0 r}$	$V(r) = -\frac{\lambda}{2\pi\epsilon_0} \ln r$	$V(x) = C - \frac{\sigma}{2\epsilon_0} x$
$\oint_S \mathbf{E} \cdot \hat{n} dA = \frac{Q_{inS}}{\epsilon_0}$	$\Delta V = \frac{Q}{C}$	$\mathbf{E} = \rho \mathbf{J}$
$ J  = \frac{I}{A}$	$U = \frac{Q^2}{2C}$	$RC = \epsilon_0 \rho$
$\mathbf{F} = q\mathbf{v} \times \mathbf{B}$	$R = \frac{mv}{qB}$	$d\mathbf{B} = \frac{\mu_0}{4\pi} I d\ell \frac{\mathbf{t} \times \mathbf{r}}{r^3}$
$V(b) - V(a) = -\int_a^b \mathbf{E} \cdot d\mathbf{r}$	$R = \frac{\rho L}{A}$	$C = \frac{\kappa\epsilon_0 A}{d}$
$\frac{d\mathbf{F}}{d\ell} = I\mathbf{t} \times \mathbf{B}$	$\oint_C \mathbf{B} \cdot d\mathbf{r} = \mu_0 I C$	$\mathbf{B} = \frac{\mu_0 q}{4\pi} \frac{\mathbf{v} \times \mathbf{r}}{r^3}$
$C_{parallel} = C_1 + C_2$	$\frac{1}{C_{series}} = \frac{1}{C_1} + \frac{1}{C_2}$	$\tan \theta = \frac{\sin \theta}{\cos \theta}$
$\mathbf{B} = \nabla \times \mathbf{A}$	$\mathbf{A}(r) = \frac{\mu_0}{4\pi} \int \frac{I d\ell \mathbf{t}}{r}$	$U = -\mathbf{m} \cdot \mathbf{B}$
$(x - x_c)^2 + (y - y_c)^2 = R^2$	$E_x = -\frac{\partial V}{\partial x}$	$E_y = -\frac{\partial V}{\partial y}$
$Q = \rho \cdot Vol$	$Q = \sigma A$	$\sigma(x) = \epsilon_0 \mathbf{E}(x) \cdot \mathbf{n}$
$F_x = -\frac{\partial U}{\partial x}$	$\mathbf{N} = \mathbf{p} \times \mathbf{E}$	$\mathbf{p} = \sum_{i=1}^2 q_i \mathbf{r}_i$
$\frac{d}{du} \tan^{-1} u = \frac{1}{1+u^2}$	$\frac{d}{dx} \frac{u}{v} = \frac{u'v - v'u}{v^2}$	$\frac{d}{dx} \ln x = \frac{1}{x}$
$\int_a^b \frac{dr}{r^2} = \frac{1}{a} - \frac{1}{b}$	$\int_a^b \frac{dr}{r} = \ln \frac{b}{a}$	$\tan(\tan^{-1}(x)) = x = \tan^{-1}(\tan(x))$
$\Delta W = \Delta(qV)$	$\frac{dW}{dVol} = \frac{1}{2} \epsilon_0 \kappa E^2$	$W = \frac{Q^2}{2C} = \frac{CV^2}{2}$
$\ln(e^x) = -\ln(e^{-x}) = x$	$V = IR$	$ma = -kx$
$Vol = \pi r^2 h$	$Vol = \frac{4\pi}{3} r^3$	$Vol = LWH$
$Area = 2\pi r h$	$Area = 4\pi r^2$	$Area = L^2$
$C = \frac{4\pi\epsilon_0 ab}{b-a}$	$C = \frac{2\pi\epsilon_0 \ell}{\ln \frac{b}{a}}$	$C = \frac{\epsilon_0 A}{d}$
$ E_{total}  = \frac{ E_{ext} }{\kappa}$	$\mathbf{J} = \frac{I}{A} \hat{n}$	$\frac{dy}{dx} = \frac{E_y}{E_x}$
$\frac{d}{dx} \tan^{-1} f(x) = \frac{f'(x)}{1+f^2(x)}$	$\tan(a-b) = \frac{\tan a - \tan b}{1 + \tan a \tan b}$	$ \mathbf{B}  = \frac{\mu_0 I}{2\pi R}, \frac{\mu_0 I}{2R}, \mu_0 n I,$
$\int_a^b \frac{dx}{(c-x)^2} = \frac{a-b}{(c-a)(c-b)}$	$U = \frac{1}{2} CV^2$	$Q = \lambda \ell$
$\frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9 \frac{Nm^2}{C^2}$	$\mu_0 = 4\pi \times 10^{-7} \frac{Tm}{A}$	$c = 3.0 \times 10^8 \frac{m}{s}$

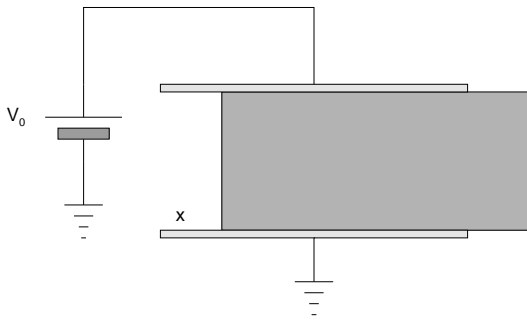


**1 (p-73) (5+5+5 points)**

A hollow ball of inner radius  $b = 2 \text{ cm}$  and outer radius  $c = 3 \text{ cm}$  is made of charged dust of density  $\rho = 1.0 \times 10^3 \frac{\text{C}}{\text{m}^3}$  contains an inner solid ball of the same matter of radius  $a = 1 \text{ cm}$ . Compute the electric field strength for  $r_0 = 0.75 \text{ cm}$ ,  $r_1 = 2.25 \text{ cm}$ , and for the exterior region,  $r_2 = 3.5 \text{ cm}$

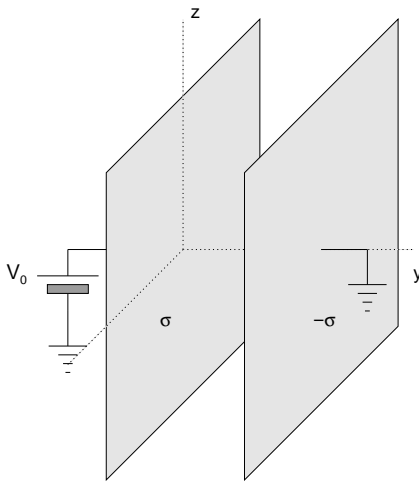
**2 (p-76) (10 points)**

A region of space around the origin contains an electric field  $\mathbf{E} = 4.0 \frac{\text{N}}{\text{m} \cdot \text{C}} x \mathbf{i} + 3.0 \frac{\text{N}}{\text{C}} \mathbf{j}$ . Such a field cannot exist in empty space. Find the total charge within a cube of side  $a = 0.5 \text{ m}$  centered on the origin, with its six faces possessing normals in the six cardinal directions  $\pm \mathbf{i}, \pm \mathbf{j}, \pm \mathbf{k}$ .



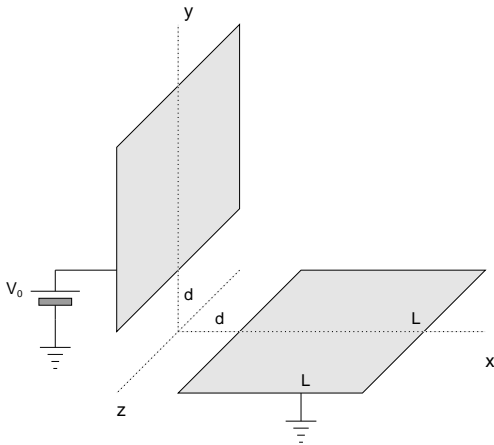
**3A. (p-109) (5+3 points)**

Consider a capacitor of plate area  $A = \ell^2 = 0.01 \text{ m}^2 = (0.1 \text{ m} \times 0.1 \text{ m})$ , separation  $d = 0.005 \text{ m}$ , connected to battery  $V_0 = 100 \text{ V}$ . A dielectric slab  $\kappa = 3.0$  fills the device. If the slab is now withdrawn by  $x = \frac{1}{3}\ell$  **compute the charge** that flows out of/into the battery. **Specify which (into/out of). Find  $|\mathbf{E}|$  (total) within the dielectric.**



**B. (p-100) (5 points)**

Consider this parallel (conducting) plate capacitor of plate area  $A = 100 \text{ cm}^2$  and plate separation  $d = 1.0 \text{ mm}$ , fringing is negligible. How much work is needed to increase the plate separation to  $3.0 \text{ mm}$ ?



**C. (e-49) (6 points)**

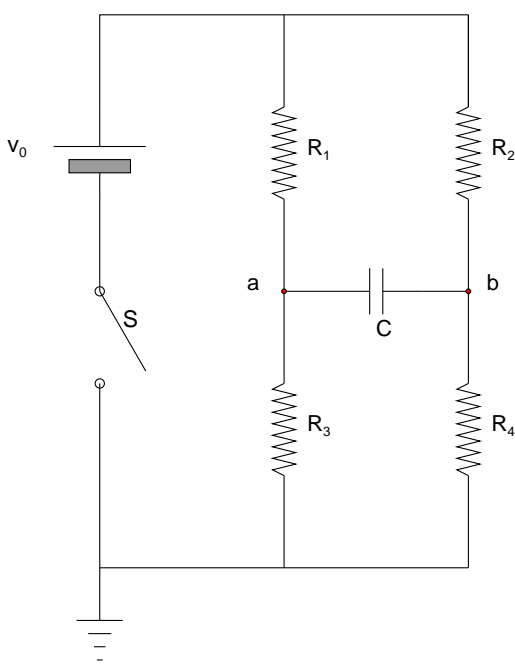
Two semi-infinite conducting planes would meet along the  $z$ -axis except for a small gap. The right horizontal plane is grounded and the left vertical is maintained at voltage  $V_0$  by a battery. The voltage function is

$$V(x, y) = \frac{2V_0}{\pi} \tan^{-1}\left(\frac{y}{x}\right)$$

Find the surface charge density  $\sigma(y)$  at a point on the left high-voltage vertical plate at a distance  $y > d$  from the  $z$ -axis.

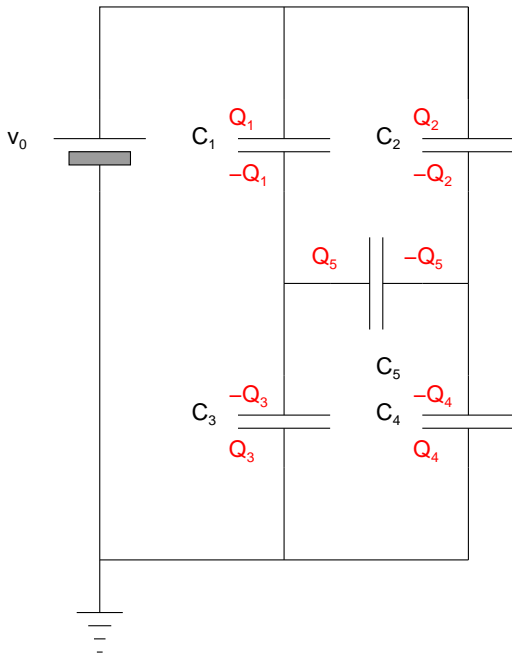
**4 A. (p-131) (2+2+2+2+2 points)**

**A.** Very long after closing the switch  $S$  at  $t = 0$ , the currents will have reached steady (constant) values, as will the charge on the capacitor. Find these steady values.  $V_0 = 100\text{ V}$ ,  $R_1 = 100\Omega$ ,  $R_2 = 200\Omega$ ,  $R_3 = 300\Omega$ ,  $R_4 = 400\Omega$  and  $C = 1.0 \times 10^{-6}\text{ F}$ . **Label your currents  $I_1, I_2, I_3, I_4$  pointing down.**

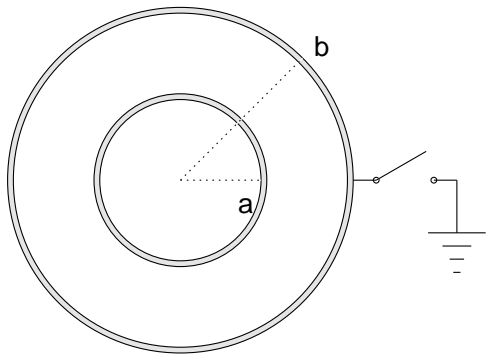


**B. (p-127) (2+2+2+2+2 points)**

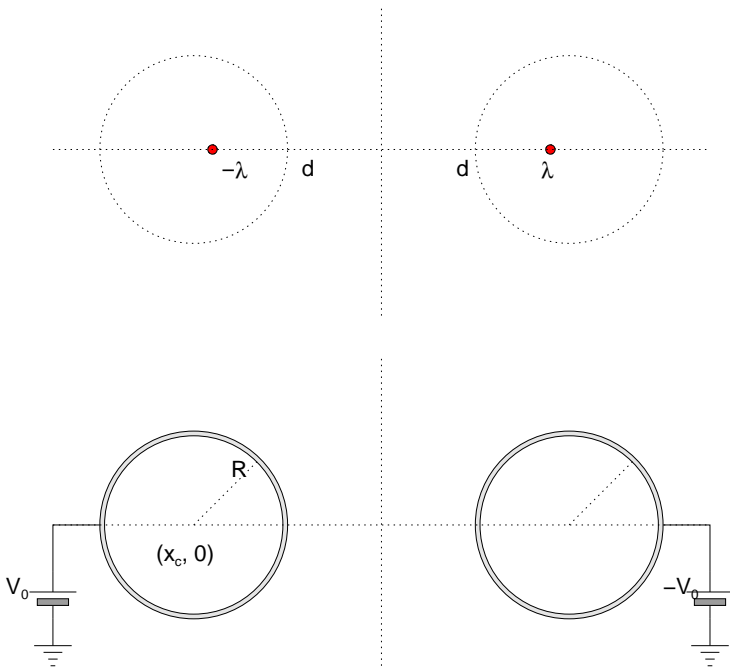
In this bridge problem we have  $V_0 = 100\text{ V}$ ,  $C_1 = C_2 = 1000\text{ pF}$ ,  $C_3 = C_4 = 5000\text{ pF}$  and  $C_5 = 3.0\text{ }\mu\text{F}$ . Find all five charges on the capacitors.



5 A. (e-58) (5+5 points)

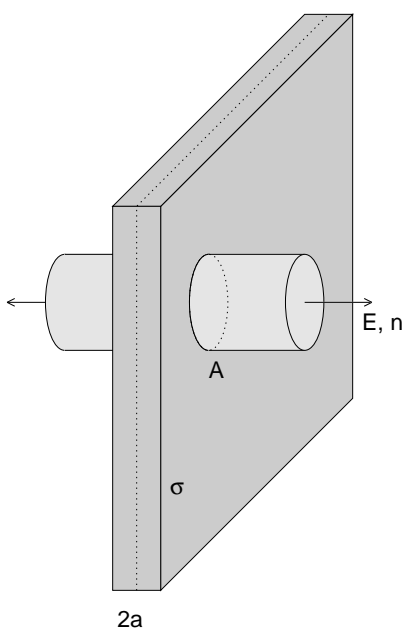


Find the capacitance of a coaxial cylindrical capacitor of length  $\ell = 2.0\text{ m}$ . Assume that the inner cylinder at  $r = a$  is connected to a battery of voltage  $V_0 = 10\text{ V}$ . Let  $a = 5\text{ cm}$ ,  $b = 6\text{ cm}$  and compute the total charge  $Q$  stored by the device.



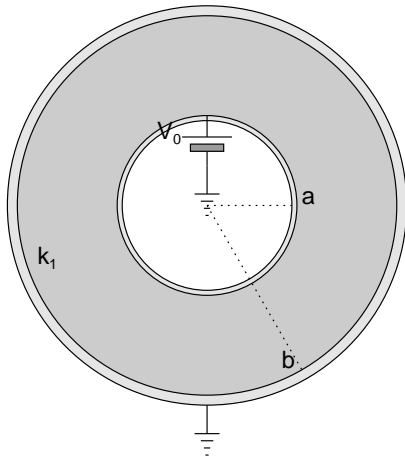
B. (p-104) (6 points)

Run the axis of a conducting cylinder of **approximately uniform** charge density  $\lambda$  and radius  $R$  parallel to the  $z$  axis through  $x = -d$ ,  $y = 0$  and run the axis of a second conducting cylinder of radius  $R$ , charge density  $-\lambda$  through  $x = d$ ,  $y = 0$  with  $d \gg R$ . The electric field between them is well approximated by replacing them with parallel line charges along their axes. Use this fact to estimate the capacitance per unit length of the two non-coaxial cylinders.



**6A. (p-84) (5+5 points)**

Compute the electric field strength at a point a distance  $x$  (measured perpendicularly) from the median plane (dotted) of an infinite planar slab of charged dust of density  $\rho$  and thickness  $2a$ , for both cases  $x < a$  and  $x > a$ .



**B. (p-118) (3+3+4 points)**

A cylindrical shell capacitor (length  $\ell$  seen in cross-section) has a layer of dielectric material with radii indicated in the figure. Find the **total electric field strength** in the dielectric as functions of  $r$ , the **molecular electric field strength** in the dielectric as functions of  $r$ , and the net **free charge** that it will pull from the battery. Answer in terms of  $a, b, \kappa_1, V_0, \ell, \epsilon_0, r$  and numbers.